

ego, California 92152

MARINE PHYSICAL ITT FILE COFY

SCRIPPS INSTITUTION OF OCEANOGRAPHY

PARABOLIC EQUATION MODEL

Jean-Marie Tran

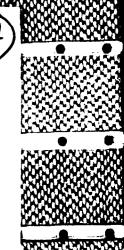
MPL TECHNICAL MEMORANDUM 401

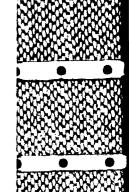
MPL-U-9/88

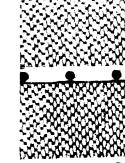
Approved for public release; distribution unlimited.

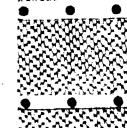
April 1988

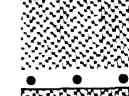














ECURITY CLASSIFICATION OF THIS PAGE	REPORT DOCUM	MENTATION A	AGE	~	
	MEPONT BOCO				
a. REPORT SECURITY CLASSIFICATION UNCLASSIFIED	* SESTRETILE MARKINGS				
28. SECURITY CLASSIFICATION AUTHORITY		3 DISTRIBUTION WEALABLETY OF REPORT			
2b. DECLASSIFICATION / DOWNGRADING SCHEDULE		Approved for public release; distribution unlimited.			
I. PERFORMING ORGANIZATION REPORT NUMBER	A(S)	1 WiOms Offices	O ASMADIN	N REPORT NUMBE	€ R(\$)
MPL Technical Memorandum 401				1	
6a. NAME OF PERFORMING ORGANIZATION	to Office States	's maune on the	,, _		
Marine Physical Laboratory	INTL MANNE)	Office of			
Sc. ADDRESS (Gty, State, and ZIP Code) University of California, San Scripps Institution of Oceans San Diego, CA 92152		** ASSMELL (CA 800 Morth Arlington	DULLTICY S	tip Cadel Lsaut	
Ba, NAME OF FUNDING SPONSORING ORGANIZATION	Bo Office Symbols	A BOW WHO A	INT "RUME IL	" IDEN" IF ICA" ICIN	NUMBER
Office of Naval Research	ONR	N00014-67	-C-0127		
8c. ADDRESS (City, State, and 219 Code)		to former or s			
Department of the Navy 800 North Quincy Street Arlington, VA 22217-5000		INTRIAL AD	MO MCHC.	* & 54 ***	WORK UNIT ACCESSION NO
11. TITLE (Include Security Classification)			<u> </u>		
PARABOLIC EQUATION MODEL					
12. PERSONAL AUTHOR(S) Jean-Marie Tran					
13a. TYPE OF REPORT 13b TIME (CO	THE DATE OF REPO			egt COUN*
Summary FROM	10	April 198			58
16. SUPPLEMENTARY NOTATION					
17. COSATI CODES	18 SUBJECT TERMS	(Continue on revers	e il necessary	and identify by	blort number)
FIELD GROUP SUB-GROUP	narabolic r	parabolic propagation model, accountic modelling,			11:50
	-	REO program	wer, ou	CANCAL PROCES	L & &1 P.J. (
19. ABSTRACT This report deals with a parabolic propagation model now suptemorand at the Marine Physical Laboratory. This parabolic equation (PE) program is a PORTRAN 77 version of the SACLANT PAREQ program (1).					
The parabolic methods were a major development in the field of accounts modeling [2]. The advantage of the method is the simple way range dependence is handled. Dif- fraction effects are included, but neither reverberation nor backscanering are accounted for [3]. The parabolic equation requires small angles of propagation from the horizontal and cannot handle steep sound velocity gradients or high frequency propagation because					
of computer speed considerations. The running time is proportional to $Hf^{2i} \frac{\partial c}{\partial z}$					
where H is the water plus bottom height, f the frequency, c the sound velocity, z the depth and R_{\max} the maximum range [4].					
cal algorithms are p Finally examples are	~	nd the program inputs	are described.		
The goal of the understand and use the	is report is to provide the pou he PE program.	ential user the necessary	information to		
20. DISTRIBUTION / AVAILABILITY OF ABSTRAC		21 ABSTRACT S		SSIFICATION	
UNCLASSIFIED/UNLIMITED SAME AS RPT. DTIC USERS UNCLASSIFIED 22a. NAME OF RESPONSIBLE INDIVIDUAL 22b TELEPHONE (Include Area Code) 22c OFFICE SYMBOL					
W.S. Hodgkiss (619) 534-1798					
DD FORM 1473, 84 MAR 83	APR edition may be used	until exhausted	SECU	RITY CLASSISICAT	ION OF THIS PAGE

PARABOLIC EQUATION MODEL

Jean-Marie Tran

Marine Physical Laboratory Scripps Institution of Oceanography San Diego, CA 92152

ABSTRACT

This report deals with a parabolic propagation model now implemented at the Marine Physical Laboratory. This parabolic equation (PE) program is a FORTRAN 77 version of the SACLANT PAREQ program.[1].

The parabolic methods were a major development in the field of acoustic modeling. [2]. The advantage of the method is the simple way range dependence is handled. Diffraction effects are included, but neither reverberation nor backscattering are accounted for [3]. The parabolic equation requires small angles of propagation from the horizontal and cannot handle steep sound velocity gradients or high frequency propagation because of computer speed considerations. The running time is proportional to $Hf^2 \left[\frac{\partial c}{\partial z} \right]_{\text{max}}^{R} R_{\text{max}}$ where H is the water plus bottom height, f the frequency, c the sound velocity, c the depth and c max the maximum range [4].

In the following pages, the parabolic equations are derived, the associated numerical algorithms are presented, the environment and the program inputs are described. Finally examples are given.

The goal of this report is to provide the potential user the necessary information to understand and use the PE program.

11 1 11

ᢣᡈᠪᢘᡌᢐᡉᢘᠪᢏᠪᢏᠪᢏᠪᢏᢒᢏᢒᢏᢒᢏᢣᡛᠵᢊᢏᠧᡎᡎᠪᠪᠪᠽᠫᠪᠪᠪᢗᠫᠪᠪᠪᠪᢓᢤᡌᢛᡌᢛᢞᡬᢣᡭᠪᢆᡫᢥᡳᢥᢣᢥᡳᢥᡫᢥᡭᡭᡫᡭᡚᡭᢥᢥᢥᢥᢥᢥᢥᢥᢥᢥᢥ



Acces	sion Fo	r /				
NTIS	GRA&I	N				
DTIC	TAB	ñ				
Unann	ounced					
Justi	fication	n				
Ву						
Distr	Distribution/					
Avai	labilit	y Codes				
	Avail a	nd/or				
Dist	Speci	al				
1	1					
0 - 1	ļ					
r		ĺ				

CONTENTS

- 1. Parabolic Approximation
- 2. Parabolic Equations
- 3. Numerical Implementation
- 4. Interpretation of the Split Step Algorithm
- 5. Description of MPL's PE Program
- 6. Phase Error Corrections
- 7. Source Field
- 8. Description and Treatement of the Environment
- 9. Program Inputs
- 10. Program Output
- 11. Examples
- 12. References

TOTAL TOTAL PROPERTY OF THE PR

1. Parabolic Approximation

The starting point of acoustic models is the homogeneous Helmholtz equation or reduced wave equation which is an elliptic partial differential equation:

$$\nabla^2 p + k^2 p = 0 \tag{1.1}$$

$$\nabla^2 p + k_o^2 n^2 p = 0 {1.2}$$

with $k^2 = k_o^2 n^2$ where k_o is a reference wave number and n can be regarded as a refraction index. In cylindrical coordinates, neglecting the azimuthal dependence, the Helmholtz equation is:

$$\frac{\partial^2 p}{\partial r^2} + \frac{1}{r} \frac{\partial p}{\partial r} + \frac{\partial^2 p}{\partial z^2} + k_o^2 n^2 p = 0 \tag{1.3}$$

Intrinsic cylindrical spreading is accounted for by a factor $r^{-1/4}$ in the pressure, leading to the classic change of variable $p = r^{-1/4}\Phi(r,z)$.

Then, the equation becomes:

$$\frac{\partial^2 \Phi}{\partial r^2} + \frac{\partial^2 \Phi}{\partial z^2} + (k_o^2 n^2 + \frac{1}{4r^2})\Phi = 0 \tag{1.4}$$

Essentially, the far field zone is of interest; therefore, $k_o r \gg 1$ is assumed with an index of refraction of the order of unity. The equation is simplified

$$\frac{\partial^2 \Phi}{\partial r^2} + \frac{\partial^2 \Phi}{\partial z^2} + k_o^2 n^2 \Phi = 0 \tag{1.5}$$

or

$$\left(\frac{\partial}{\partial r^2} + k_o^2 Q^2\right) \Phi = 0 \tag{1.6}$$

where the operator Q is

$$Q^{2} = n^{2} + \frac{1}{k_{0}^{2}} \frac{\partial^{2}}{\partial z^{2}}$$
 (1.7)

Parabolic approximations are obtained by factorization of the differential operator Q into the product of two commuting operators

$$\left(\frac{\partial^2}{\partial r^2} + k_o^2 Q^2\right) = \left(-i\frac{\partial}{\partial r} + k_o Q\right) \left(i\frac{\partial}{\partial r} + k_o Q\right) \tag{1.8}$$

It requires that $\frac{\partial}{\partial r}$ and Q commute. This condition is considered satisfied if the index of refraction slowly varies in range so that the gradient $\frac{\partial n}{\partial r}$ is negligible.

The differential equation then can be separated into two equations:

$$(i\frac{\partial}{\partial r} + k_o Q) \Phi = 0 \tag{1.9}$$

$$(-i\frac{\partial}{\partial r} + k_o Q) \Phi = 0 \tag{1.10}$$

The general solution is the sum of their two solutions, the first one represents the outgoing wave and the second one the incoming wave. The underlying nature of the parabolic approximation is to consider that the solution propagates primarily in the outward direction with very little reflection, backscattering and reverberation.

2. Parabolic Equations

<u>ŗĸċĸŗĸŗĸċĸċĸċĸċĸċĸċĸċĸċĸċĸ</u>?₽ĊĠĊĸŶŶŶĠĊŶĊŶĊŶŎ

The differences in formulations of the parabolic approximations leading to different parabolic equations reside in the way the Q operator is evaluated. The pseudo differential operator Q is rewritten as

$$Q = (1+n^2-1+\frac{1}{k^2}\frac{\partial^2}{\partial z^2})^{\nu_2}$$
 (2.1)

and linearized in different ways by assuming either $(n^2-1)\Phi$ or $\frac{1}{k_o^2}\frac{\partial^2\Phi}{\partial z^2}$ is small compared to Φ .

Taking $n^2-1 \ll 1$ is equivalent to considering small gradients of the sound velocity. Tappert [6] shows that the term $\frac{1}{k_o^2} \frac{\partial^2 \Phi}{\partial z^2}$ is related to the mean square angle of propagation with respect to the horizontal. If $\Phi = \exp ik_o (r\cos\theta \pm z\sin\theta)$, the norm of $\frac{1}{k_o^2} \frac{\partial^2 \Phi}{\partial z^2}$ is $\sin^2\theta$ where θ is the angle of propagation with respect to the horizontal. Therefore assuming it is small is equivalent to considering small propagation angles with respect to the horizontal.

Approximations of the Q operator lead to two classes of models, one of iterative methods based on finite difference schemes, the other based on the Split Step Algorithm [6,7] using Fast Fourier Transforms (FFTs). Only the last class will be described here in relation to MPL's PE program.

The standard small angle parabolic approximation is obtained by assuming that both the index of refraction term and the propagation angle term are small and by using a first order Taylor series [5,6].

$$Q = \left[1 + \frac{n^2 - 1}{2} + \frac{1}{2k_o^2} \frac{\partial^2}{\partial z^2}\right]$$
 (2.2)

The corresponding equation is obtained by the classic transformation $\Phi = e^{i \mathbf{k} \cdot \mathbf{r}} \Psi$:

$$i\frac{\partial}{\partial r}(e^{ik_{\sigma}r}\Psi)+k_o\left[1+\frac{n^2-1}{2}+\frac{1}{2k_o}\frac{\partial^2}{\partial z^2}\right](e^{ik_{\sigma}r}\Psi)=0$$
 (2.3)

$$i\frac{\partial\Psi}{\partial r} + k_o \frac{n^2 - 1}{2} \Psi + \frac{1}{2k_o} \frac{\partial^2\Psi}{\partial z^2} = 0$$
 (2.4)

$$\frac{\partial^2 \Psi}{\partial z^2} + 2ik_o \frac{\partial \Psi}{\partial r} + k_o^2 (n^2 - 1)\Psi = 0$$
 (2.5)

Equation (2.5) is the standard parabolic equation, also called Tappert and Hardin parabolic equation.

Thompson and Chapman [7] introduced an improved parabolic approximation by using another development of Q proposed by Feit and Fleck [8];

$$Q = \sqrt{1 + \frac{1}{k_a^2} \frac{\partial^2}{\partial z^2}} + \sqrt{1 + n^2 - 1} - 1$$
 (2.6)

$$Q = \sqrt{1 + \frac{1}{k_o^2} \frac{\partial^2}{\partial z^2}} + n - 1$$
 (2.7)

They showed that this approximation can stand much wider angles. While the standard parabolic equation is valid to about $\pm 20^{\circ}$, this modified parabolic equation is valid up to $\pm 40^{\circ}$ [4]. Using an additional pseudo-operator identity

$$(1+\mu)^{N_2} = 1 + \frac{\mu}{(1+\mu)^{N_2}+1}$$
 (2.8)

the equation becomes

$$i\frac{\partial\Phi}{\partial r} + k_{\sigma} \left[1 + \frac{\frac{1}{k_{\sigma}^{2}} \frac{\partial^{2}}{\partial z^{2}}}{\left(1 + \frac{1}{k_{\sigma}^{2}} \frac{\partial^{2}}{\partial z^{2}}\right)^{1/4} + 1} + n - 1 \right] \Phi = 0$$
 (2.9)

With the previous envelope transformation $\Phi = e^{i\Phi_r} \Psi$, one gets

$$i\frac{\partial\Psi}{\partial r} + k_o \frac{\frac{1}{k_o^2} \frac{\partial^2\Psi}{\partial z^2}}{(1 + \frac{1}{k_o^2} \frac{\partial^2\Psi}{\partial z^2})^{1/4} + 1} + k_o (n-1)\Psi = 0$$
(2.10)

3. Numerical Implementation

These parabolic equations are extensively used because of their efficient numerical implementation based on FFTs. Jensen and Krol [2,9] elegantly derive the Split Step algorithm for the Tappert and Hardin parabolic equation. They do its Fourier transform and assume an almost constant index of refraction. By inverse Fourier Transform, they get

$$\Psi = e^{i\frac{k_{o}}{2}(a^{k}-1)(r-r_{o})}F^{-1}\left[e^{\frac{i(r-r_{o})z^{1}}{2k_{o}}}F(\Psi(r_{o},z))\right]$$
(3.1)

where F is the one dimensional Fourier transform with respect to z, r_o is a reference range, and s is the Fourier variable.

The above algorithm was primarily derived by Tappert and Hardin [5,6] using operator representations. The parabolic differential equation is

$$\frac{\partial \Psi}{\partial r} = iA \, \Psi + iB \, \dot{\Psi} \tag{3.2}$$

with $A(r,x) = \frac{k_0}{2}(n^2-1)$ and $B(z) = \frac{1}{2k_0} \frac{\partial^2}{\partial z^2}$. Note that at this point, attenuation can

be introduced by inserting a complex term in $A: A = \frac{k_o}{2}(n^2-1+i\alpha)$. The solution is then assumed to be

$$\Psi(r_o + \Delta r, z) = \left[\exp \left\{ i \int_{r_o}^{r_o + \Delta r} A(r, z) dr + i \int_{r_o}^{r_o + \Delta r} B(z) dr \right\} \right] \Psi(r_o, z)$$
(3.3)

by analogy with differential equations in the real space with constant coefficients A.B. Assuming that A varies slowly with respect to r, on splits the operator $\Psi(r_o + \Delta r.z) = \exp(i \Delta rA) \exp(i \Delta rB) \Psi(r_o.z)$. The term $\exp(i \Delta rB) \Psi(r_o.z)$ is evaluated via its Fourier transform

$$exp(i\Delta rB)\Psi(r_o,z) = F^{-1}\left[e^{-i\frac{\Delta r}{2k_o}}F\left[\Psi(r_o,z)\right]\right]$$
(3.4)

One can easily derive the Split Step Algorithm for the modified parabolic equation (Thomson and Chapman):

$$\Psi(r,z) = e^{i\frac{k_o}{2}(n-1)(r-r_o)} F^{-1} \left[\exp\left[\frac{-i\frac{s^2}{2k_o}(r-r_o)}{(1-\frac{s^2}{k_o^2})^{1/2}+1} \right] F\left[\Psi(r_o,z) \right] \right]$$
(3.5)

CONTRACTOR SERVICES S

4. Interpretation of the Split Step Algorithm

Two physical phenomena are involved: the propagation in a homogeneous environment and the influence of changes in the medium on the propagation. The Split Step Algorithm multiplies the angular spectrum by a phase shift to account for propagation over a range step Δr . The steeper the angle, the greater is the phase shift. Then it multiplies the inverse Fourier transform of this new range step spectrum by the index of refraction term which accounts for changes in the medium.

Other algorithms for the standard parabolic equation were introduced [6,10] such as

$$\Psi(r_{o} + \Delta r_{o}x) = \exp\left[\frac{i\Delta rk_{o}(n^{2}-1)}{4}\right]F^{-1}\left\{\exp\frac{i\Delta rx^{2}}{2k_{o}}\left[F\left(\exp\left(\frac{i\Delta rk_{o}(n^{2}-1)}{4}\right)\Psi(r_{o}x)\right)\right]\right\}$$
(4.1)

It allows for a better coupling between the two physical phenomena described above. An error analysis [10] shows that the initial algorithm (3.1) has a second order accuracy in r while the last one (4.1) has a third order accuracy in r

The Split Step Algorithm is a marching solution in range, therefore range dependence of the environmental data (sound velocity profiles, bathymetry) is easily introduced. Boundary conditions are implicit in the numerical solution. A pressure-release surface at the air/water interface is assumed, the field is made anti-symmetrical in depth about z=0 by using real sine transforms [10]

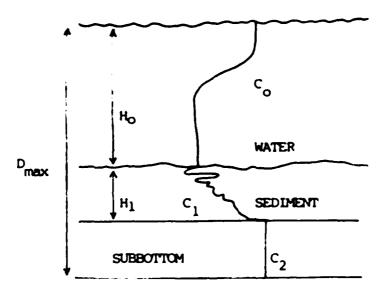
The Fourier theory assumes L^T integrable functions, the field must vanish below the maximum depth of the transform. A pressure release bottom must correspond to the maximum transform sample to avoid aliasing while doing FFTs.

An unphysical bottom layer is introduced to attenuate the field in the bottom [10]. This technique assures that at long range, the dominant contribution comes from low order modes that correspond to low grazing angle. The higher the mode, the greater is the grazing angle, and the more penetration into the bottom.

15555555 - 155555551

5. Description of MPL's PE Program

The algorithms used are the Split Step Algorithms (3.1) and (3.5) which have a second order accuracy in r. The initial transform size is determined by the input transform component N, the transform has a total of 2^N points. N must be smaller than 12. The maximum depth of the transform Z_{max} is the maximum depth of the bottom D_{max} extended by a factor of 33 % to account for the unphysical attenuating layer.



If the input transform size is not given, it is determined by the program using

$$N = 1 + \log_2(kZ_{\text{max}}/2) \tag{5.1}$$

where k is the average wave number, and Z_{max} is the maximum depth transform.

The program begins by creating the starting field and, in a range loop, reads the environmental data, creates the refraction index table, $e^{i\Delta rA}$, and the second derivative table, $e^{i\Delta rB}$. If the range step is not fixed, the program computes a new range step at each range: $\Delta r = \frac{\lambda}{1-\cos\theta}$ where λ is the wavelength and $\theta = \tan^{-1}\left[\frac{|sF(\Psi)|}{k_o|F(\Psi)|}\right]$, s is the Fourier variable, F is the Fourier transform and $|\cdot|$

is the L^2 norm (i.e. $|F| = \int_{-\infty}^{\infty} FF^* ds$).

If the new range step has a relative difference with respect to the old range step of at least 25% then this new range step is selected and a new table of second derivatives $e^{i \Delta n \theta}$ is computed. Otherwise, the old range step and the second derivative table are kept. The program does Fourier sine transforms and multiplies the transformed field by the table of second derivatives:

$$\exp\left[-i\frac{\Delta r_{apo} + \Delta r_{abd}}{2} \frac{s^2}{2k_a}\right] \quad (standard PE)$$
 (5.2)

$$\exp\left[-i\frac{\Delta r_{ann} + \Delta r_{old}}{2} \frac{\frac{j^2}{2k_n}}{\left(1 - \frac{j^2}{k_n^2}\right)^{n_0} + 1}\right] \quad (modified PE) \tag{5.3}$$

The inverse sine Fourier transform is performed and the field is then multiplied by

$$\exp\left[i\frac{\Delta r_{\text{now}}}{2}(n^2-1)\right]e^{-nr_{\text{obs}}} \quad \text{(standard PE)} \tag{5.4}$$

$$\exp\left[i\frac{\Delta r_{\text{con}}}{2}(n-1)\right]e^{-\Delta r_{\text{con}}} \quad (Modified PE)$$
 (5.5)

 α is the attenuation in the water or in the bottom. The program advances the range to $r = r_{odd} + \Delta r_{max}$.

After bookkeeping on the range dependence of the environment is completed, it checks for aliasing in the transform. Aliasing occurs when the contribution of steep angles in the angular spectrum is significant. The parabolic approximation is based on the "small angle" hypothesis. The angular spectrum is divided into four equal bins, their energy, E_1 , E_2 , E_3 , E_4 from low to high angles are computed. An aliasing factor is defined as $10 \log_{10} R_1$ with $R_1 = \frac{E_4}{E_1 + E_2 + E_3 + E_4}$. If $-14 \, dB < R_1$, then the energy is spread throughout a large

angular interval and aliasing is severe so the run is terminated. If $-20 \, dB < R_1 < -14 dB$, then a warning is issued and after five warnings the run is terminated. Two oversampling factors are defined, $R_2 = \frac{E_3 + E_4}{E_1 + E_2}$ and $R_3 = \frac{E_1}{E_2}$. If $R_2 < -70 \, dB$ and $R_3 < -60 \, dB$, the field is oversampled and the transform size is reduced by a factor of 2.

6. Phase Error Corrections

The parabolic approximation and the Split Step Algorithm are applicable if the index of refraction locally varies only slightly and if propagation is limited in a narrow aperture about the outward range.

Comparison between the parabolic equation and elliptic equation normal mode phase velocities in range independent waveguides [11,12] showed that the parabolic approximation introduces phase errors.

In the case of a single normal mode describing the propagation, the phase error is canceled if the reference wave number, k_o , is chosen to be the mode wave number [11]. When several modes are propagating, there is no obvious a priori choice for k_o [13] even if it can be intuitively understood as a weighted sum of the excited mode wave numbers [12]. In practice, the choice of k_o is left to the model user. Two different methods implemented on MPL's PE program try to correct these phase errors.

The first method by Brock et al [14], also called the CMOD correction, modifies the environment, i.e. the profile of the refraction index to minimize the phase errors. The idea is to decompose the sound field calculated by the parabolic equation into propagating normal modes and to compare these modes with those obtained by a WKB approximation to the elliptic wave equation. Requiring that the depths of the modal turning points (where the mode amplitudes are the largest) are the same in the parabolic and elliptic cases, that the phase velocities at the turning points are the same and assuming that there is no isovelocity region, a mapping can be derived:

$$(n,z) \to (\sqrt{n^2-1}, z\sqrt{n}) \tag{6.1}$$

The CMOD correction appears to offer improvements when the source and the receiver are near the surface, the bottom, or in regions near individual mode turning points.

Pierce introduced a better approach to determine in a more natural way the reference wave number by using the Rayleigh Principle: "if the propagation is progressive such that the energy is being transported on the average in one direction without propagation in the backward direction then the average kinetic energy is equal to the average potential energy" [13].

The kinetic energy in the volume element, V_o , is $\frac{1}{2}\rho\left(|u|^2+|v|^2\right)V_o$ where u,v are the particle velocities in the r,z directions respectively. The potential energy is $-\int P\ dV$ where P is the pressure and dV is the change of volume of the volume element with varying pressure. If the volume element dimensions are small compared to the wavelength, the plane wave approximation can be used and $V = V_o\left(1 - \frac{P}{\rho c^2}\right)$ and therefore, $dV = -\frac{V_o dP}{\rho c^2}$. Then, the potential energy becomes $\frac{P^2V_o}{2\rho c^2}$ [15].

Using a volume element integrated over z, the Rayleigh Principle becomes

$$\int \frac{1}{2} \rho(|u|^2 + |v|^2) dz = \int \frac{1}{2} \frac{P^2}{\rho c^2} dz$$
 (6.2)

This principle can be applied in underwater acoustics where the field is a superposition of modes [13]. The equation becomes

$$k_o^2 = \frac{\int (\frac{\omega}{c})^2 \rho^{-1} |\Phi|^2 dz - \int \rho^{-1} |\Phi_z|^2 dz}{[\rho^{-1} |\Phi|^2 dz}$$
(6.3)

since

$$|u|^2 = \left(\frac{k_o}{\omega \rho}\right)^2 \frac{|\Phi|^2}{r} \tag{6.4}$$

$$|v|^2 = \left(\frac{1}{\omega \rho}\right)^2 \frac{|\Phi_z|^2}{r}$$

$$|P|^2 = \frac{|\Phi|^2}{r}$$

$$\Phi_z = \frac{\partial \Phi}{\partial z}$$
(6.5)

$$|P|^2 = \frac{|\Phi|^2}{r} \tag{6.6}$$

$$\Phi_t = \frac{\partial \Phi}{\partial \tau} \tag{6.7}$$

This wave number is range dependent and can be proved to be range independent in range independent media. The method also allows discontinuities of density. The natural choice for k, as given by Pierce consistently yielded more accurate results than when other schemes were used [13]. According to [1], it is strongly recommended, to ensure maximum accuracy of the PE calculations, to use this phase velocity correction together with the modified parabolic equation (Thomson and Chapman). MPL's PE program computes k_o every ten range steps.

IN ECONOCIAL SENECIAL EXCESSED ENVIORS HOWEVER BOSCOCKE DOWNERS DEPOSITE DESCRIPTION OF THE PROPERTY OF THE PR

7. Source Field

Initial fields must be computed to start the marching solution in range. The wave equation to solve is

$$\frac{\partial^2 p}{\partial r^2} + \frac{1}{r} \frac{\partial p}{\partial r} + \frac{\partial^2 p}{\partial z^2} = -\frac{2p_o}{r} \delta(r) \delta(z - z_o)$$
 (7.1)

where p_o is the pressure at one meter [6]. p_o is set to unity.

The starting field can be either created by source routines available in the program or entered as an input in a file. The three available sources are the Gaussian source [6], the Greene source [16] and the Thomson source [7].

The Gaussian source is an asymptotic approximation to spherical spreading in the far field. The standard parabolic equation is simplified in the near field by neglecting the refraction term;

$$2ik_o \frac{\partial \Psi}{\partial r} + \frac{\partial^2 \Psi}{\partial z^2} = 0 \tag{7.2}$$

with $p=r^{-1/2}e^{ik_z r}\Psi$. Near the point source at depth z_s , the field is spherically spreading $p=\frac{e^{ik_z R}}{R}$ with $R=\sqrt{r^2+(z-z_s)^2}$. To do an asymptotic matching between the two expression for p, one lets $r\to\infty$ in the spherical spreading solution and, after a first order expansion:

$$p = \frac{1}{r}e^{ik_0r(1+\frac{(z-z_s)^3}{2r^3})} \left[1 - \frac{1}{2}\frac{(z-z_s)^2}{r^2}\right]$$
(7.3)

Taking the solution of the simplified parabolic equation, one lets $r \to 0$, and by asymptotic connection one gets

$$\Psi(0,z) = \frac{1}{\sqrt{r}} e^{\frac{ik_r(z-z_r)^2}{2r}}$$
 (7.4)

This solution given by Tappert is simple and avoids spurious sidelobes [5,6]. This source has been modified to allow some tilt with respect to the horizontal. The half width θ_1 of the source (half angle corresponding to a 3 dB loss with

respect with the center of the source) can be selected too. Taking $\theta_1 = 0$ corresponds to the original source or the standard Gaussian source, that is to a half width of 35°.

The Greene source is documented in [16]. It has been designed for a higher angle parabolic equation (HAPE). It is a wide angle source with a -3 dB half width of 80°.

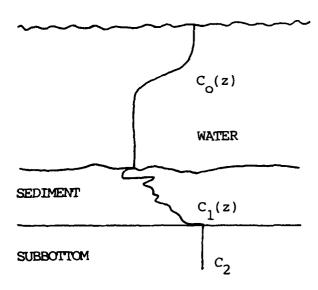
The Thomson source is an alternate starting field that uses a Kaiser Bessel window to design a source that insonifies a limited aperture in the k_1 space. The parameters describing this source are the depth of the source z_2 , the half width of the source aperture θ_1 , the tilt of the source θ_2 and α the level in dB between the stopband and the passband in the k_2 space. The field is

$$\Psi(0,z) = \left(\frac{c_o}{f}\right)^{1/2} \frac{1}{\pi(z-z_s)} \sin[2\pi \frac{f}{c_o}(z-z_s)\tan\theta_1] \frac{I_o(xy)}{I_o(x)} e^{2\pi \frac{f}{c_o}(z-z_s)^2 \sin\theta_1}$$
(7.5) with $x = 0.1102$ (\$\alpha - 21\$) and \$\alpha > 50\$. The Thomson source as implemented in PE uses \$\alpha = 60\$ so $x = 4.2978$. I_o is the modified Bessel function of 0^{th} order. $y = \left(1 - \left[\frac{z-z_s}{Z_{max}-z_s}\right]^2\right)^{1/2}$ where Z_{max} is the maximum transform depth and c_o is the reference sound speed.

The PE program can also be started by a source field stored in a file. The file must have 2^N pairs of the real and imaginary parts of the pressure. Each pair corresponds to the pressure field at a point of the mesh which has a depth increment equal to $\frac{Z_{\text{max}}}{2^N-1}$, where Z_{max} is the maximum depth of the transform. This field should be normalized such that the field corresponds to a unit pressure source at one meter, and be a solution of (7.1). The Gaussian source and the Thomson source have been properly normalized.

8. Description and Treatment of the Environment

The treatment of the environment is described in the documentation of the SACLANT PE program [1]. The bottom is a two layer fluid bottom: a sediment layer characterized by a height, an arbitrary sound velocity profile, a density, and a compressional wave attenuation, and a subbottom layer characterized by a sound velocity, a density and a compressional wave attenuation.



The change of density between the various layers (water, sediments, subbottom) is taken care of by the method given by Tappert [6]. The correct wave equation is

$$\rho \nabla (\frac{1}{\rho} \nabla p) + \frac{\omega^2}{c^2} p = 0 \tag{8.1}$$

where ρ is the density. By doing the change of variable $q = \frac{p}{\sqrt{\rho}}$, the equation becomes

$$\nabla^2 q + k_o^2 n^2 q = 0 \tag{8.2}$$

where $k_o = \frac{\omega}{c_o}$ and n is an effective index of refraction:

$$n^{2} = \frac{c_{o}^{2}}{c^{2}} + \frac{1}{2k_{o}^{2}} \sqrt{\rho} \nabla (\rho^{\frac{-3}{2}} \nabla \rho)$$
 (8.3)

The discontinuities of the density are not allowed and the program smears out its jumps. If the density jumps from ρ_1 to ρ_2 , the smoothed density is

$$\rho(z) = \frac{(\rho_1 + \rho_2)}{2} + \frac{(\rho_2 - \rho_1)}{2} \tanh(\frac{z - h}{L})$$
and L is taken such that $L = \frac{2}{k_0}$. (8.4)

The subbottom has a height twice the wavelength. If the phase velocity of the subbottom is set to zero, this height is also zero and there is no subbottom.

Bottom loss is introduced by adding a small imaginary part to the wave number [2], $k = k_R + i\alpha$ with $\alpha \ll k_R$ where $k_R = \frac{\omega}{c}$. This attenuation is expressed as part of the refraction index $n^2 = (\frac{c_o}{c})^2 + i(\frac{c_o}{c})^2 \frac{2c\alpha}{\omega}$, assuming that $\alpha \ll \frac{\omega}{c}$. The imaginary part of the refraction index is then expressed in term of the real part $n_I^2 = \frac{2\alpha c}{\omega} n_R^2$. The actual input for the attenuation is β in dB/λ where λ is the wavelength. Then $\alpha = \beta \frac{\omega}{2\pi c (20\log e)}$ and $n_I^2 = \frac{\beta}{27.287527} n_R^2$.

Volume attenuation in the water is introduced by multiplication of the field by a term $e^{-\alpha r}$ [1] but this term is fairly low at the frequencies of interest for PE, that is below 200 Hz.

Since the environment can vary in range, one must provide the program with sets of the environmental data at specified ranges. A sector is defined by these riggs associated with environmental data. In each sector, the sound velocity profile is range independent while the bathymetry is linearly interpolated in range between the two ends of the sector (water depth, sediment depth, subbottom depth). The sound velocity profile is interpolated linearly with depth. However the sound velocity profile will jump from one sector to another because it is not interpolated in range.

9. Program Inputs

The program has a readable input file. Data can be divided into two groups. One has the general information such that frequency, source depth, filenames for output results. The other contains environmental information that must be repeated for each sector. A list of the inputs follows. All of the following information must be included or lines left blank.

A1. Title of the input file or run

A2. five output filenames of seven characters each where the output will be dumped (sector information file, transmission loss versus range at selected receiver depths, transmission loss versus depth at selected ranges, SIO data file for subsequent use for contour plot and SIO outfilename for the pressure field). If blank, no file is generated.

A3. Transform size (integer smaller or equal to 12), 0 meaning that the program itself will compute the transform size based on a sufficient sampling for the Gaussian source.

A4. Reference sound speed (allowing the calculation of k_o). A negative sound speed means that the Pierce phase correction will be used. A nul sound velocity means that the CMOD correction will be used. Otherwise the given sound velocity will be used as reference sound velocity in the calculation of the index of refraction, and its value must have a physical value (e.g. $1500 \, m/s$).

A5. Output range step size (in m). It must be greater than the range step.

A6. Frequency (in Hz) since at high frequency the range step is small, the frequency should be taken below 200 Hz.

A7. Source depth (in m)

- A8. Maximum range of track (in km)
- A9. Parabolic equation flag; 0 means that the standard parabolic equation will be used, 1 means that the modified parabolic equation will be used.
- A10. Spreading flag; 0 means that the source is a point source in a 3-D geometry while 1 means that the source is a line source in a 2-D geometry (i.e. a horizontal line source perpendicular to the range-depth plane).
- A11. Source flag; 0 means that the starter will be the Gaussian source, 1 the starting field is provided by the user in a file, 2 the starter is the Greene source and 3 the starter is the Thomson source.
- A12. Half beam width and Beam tilt (up is positive) with respect to the horizontal (in degrees) for source flag equal to 0, 2, 3.
- A13. Filename containing the starting field when it is provided as input (source flag equal 1).
- A14. Number of receiver depths and number of selected ranges (each one ≤ 20) where transmission loss is desired.
- A15. Number of ranges and number of depths for the contour plot (maximum dimension of 100 for each).
 - A16. List of the receiver depth array (m) in increasing order
 - A17. List of the selected ranges (m) in increasing order
- A18. Number of sectors (the environmental data must be repeated for each sector)
 - B1. Water depth (in m) and starting range of the sector (in km)
 - B2. Number of points in the water sound velocity profile

- B3. List of pairs depth, sound velocity (in m and m/s)
- B4. Sediment height in m and density (in g/cm³)
- B5. Attenuation in the sediments (in dB/λ)
- B6. Number of points in the sediment sound velocity profile
- B7. List of the couples height, sound velocity (in m and m/s)
- B8. Subbottom density (in g/cm^2), attenuation (in dB/λ)
- B9. Subbottom sound velocity (in m/s)

When two arguments are on the same line, be sure to have at least one space (not a comma) in between. The couples height/sound velocity must be such that the first sound velocity value corresponds to a zero height and the last one to the maximum height. Also note that heights are used and not depths for the sediment layer.

10. Program Output

The user is allowed in the input file to ask for five different outputs:

- a sector information file that summarizes all environmental information
- a transmission loss versus range file that contains the transmission loss versus range for each receiver depth over the entire range of track. A multichannel SIO data file is automatically created for subsequent processing and plotting. The name of this SIO data file is the inputed filename with the "sio" extension. The first channel of the file contains the ranges and the following ones (up to 20) correspond to a receiver depth and contain the transmission loss.
- a transmission loss versus depth that contains the transmission loss versus depth for each selected range, over the maximum physical depth. A multichannel SIO data file is automatically created for subsequent processing and plotting. The name of this SIO file is the inputed filename with a "sio" extension. The file is structured in pair of channels where the $2p-1^{th}$ and the $2p^{th}$ channel correspond to the depth and the transmission loss of the p^{th} selected range.
- a SIO data file to feed a contour routine. This file has a number of channels equal to the number of depth samples (A15). Each channel has a number of points equal to the number of ranges samples (A15). The file is an equi-spaced grid in range and depth of transmission loss values.
- a SIO data file containing the pressure field where the first channel contains the real part of the pressure and the second one the imaginary part of the pressure. This output requires a fixed range step and a fixed transform size N. Each channel is made of sequential 2^N point segments; Each segment corresponds to a range sample.

11. Examples

11.1. Isovelocity Shallow Water (Range Independent)

The first example is a shallow water run taken from [1]. The medium is range independent with isovelocity water and bottom, but without subbottom. The source used is the standard Gaussian source (half bandwidth of 35°) at a depth of $25 \, m$. The frequency is $50 \, Hz$. The standard parabolic equation is used with a reference sound speed equal to $1500 \, m/s$. No phase velocity correction is applied. A copy of the script, the input file and the plot control files are presented below. In this example two modes are propagating, one with a stronger attenuation than the other. We find the same transmission loss versus range plot as in [1]. This run takes 15 minutes on a Sun Worksation 3/50 (Sun Workstation is a registered trademark of Sun Microsystems, Inc).

```
Apr 19 16:40 1988 scr Page 1

EXAMPLE 1

pe << INN
example. 1

INN
framsform the range from meter unit into km unit
demax 1 outfill2sio templ
demax 2 outfill2sio templ
demax 2 outfill2sio templ
demax 2 outfill2sio templ
mix temp templ templ
mix temp templ templ
framsform No sexample.pitl
fram.com
outfill2siobis
noutfill2siobis
framsform example.pitl
fram.com
outfill2siobis
framsform framsform
```

```
number of receiver depths, of selected ranges for ti vs range or depth
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          number of points in the water sound velocity profile (integer)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            source 0=gaussian, 1=field given in file, 2=greene, 3=thompson
                                                                                                                                                                                                                                                                                                                                                                               transmission loss versus range at selected depths transmission loss versus depth at selected ranges
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 flag for geometry (0=3-D point source,1=2-D line source)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             input filename containing the starting field (source=1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         operational mode of parabolic equation model (0 or 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        half beam width, beam tilt from horizontal in degrees
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   sound velocity profile : depth in m, velocity in m/s
                                                                                                                 input file for the program pe (MPL's pareq version)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    number of ranges, number of depths for contour plot
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 sediment heigth in m, sediment density in g/cm**3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               tranform size (0 means that pe takes care of it)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            input receiver depth array for tl vs range in m
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    input selected range array for tl vs depth in m
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   reference sound speed in m/s (can be 0, <0, >0)
                                                                                                                                                                                                                                                                     # enter the 6 file names to save the output data
####### 7 characters is the required format
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        range step (0 means it is variable in pe)
                                                                                                                                                                                                                                                                                                                                                                                                                                                    contour data in sio data file
filed data sio data file
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  water depth in m, starting range in km
                                                                                                                                                                                                                                                                                                                                                    sectors information file
Apr 19 16:43 1988 example.1 Page 1
                                                                                                                                                                                                                                  : Shallow Water
                                                                                                                                                                                         title of the input data file
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       maximum range of track in km
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         number of sectors (integer)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           output range distance in m
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          repeat for each sector :
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            source depth in m
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       frequency in Hz
                                                                                                                                                                                                                                  Saclant Test #1
                                                                                                                                                                                                                                                                                                                                                                               outfil2
```

```
Apr 19 16:43 1988 example.1 Page 2
```

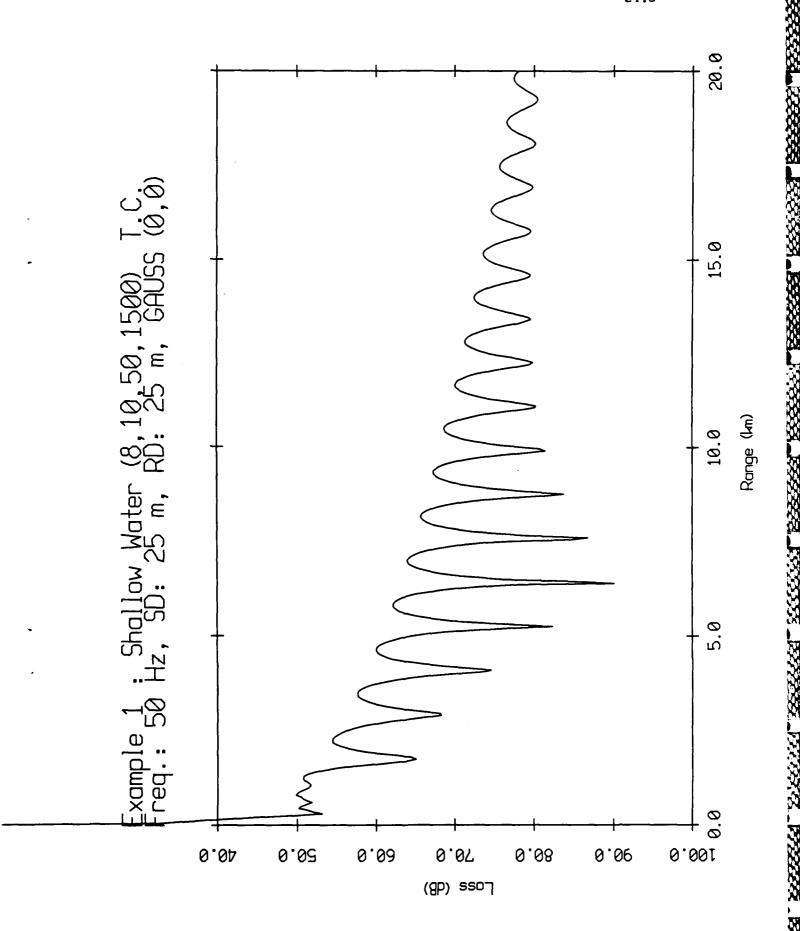
attenuation in sediment in dB/wavelength
0.5
number of points in the sediment sound velocity profile (integer)
2
sound speed profile in sediment : depth in m, velocity in m/s
0.
1500.
250. 1600.
subbottom density in g/cm**3 and attenuation in dB/wavelength

0.
sound velocity in subbottom m/sec
0.

3		0.0 A				
GOVED DA		AT RANGE				
-	-	# #				
a comment	DEPTH(M) SPEED(M/S) 0.00 1500.00 100.00 1500.00	SOUND SPEED PROFILE IN SEDIMENT # DEPTH(M) SPEED(M/S) 0.00 1600.00 250.00 1600.00	SEDIMENT DENSITY = 1.500 SEDIMENT ATTENUATION = 0.500 NO SUBBOTTOM			
10000	SPEE	PROFILE SPER 16	NSITY = TENUATIC M			
	DEPTH(M) 0.00 100.00	OUND SPEED DEPTH(M) 0.00 250.00	DIMENT DE DIMENT AT SUBBOTTO			

GIORAL PLOT CONTROL PARMETERS 1, numpit number of data files plotted on one plot 2, kler-x axis learch in inches plotted on one plot 3, kler-x axis learch in inches (1) box, (2) lower, (3) mid (6) 4, nafe-x axis suppression, (0) supress, (1) box, (2) lower, (3) mid (6) 5, nafe-x axis origin in user units 4, Axis CALINKO PARAMETERS 50, xonax-x maximum in user units 6, xinc-x tic mark spacing in user units 7, xinc-x tic mark spacing in user units 8, xinc-x tic mark spacing in user units 1, xinc-x minimum in user units 1, xinc-x tic mark spacing in user units 1, number spacing in user units 2, yien - lower left corner x position 1, yien - lower left corner y position 2, dec justify 2, dec justify 2, dec justify 3, size exponential control 3, yien - length of axis exponential control 4, yien - length of axis exponential 5, yien - length where (8, 10, 50, 1500) T.C. 1, nucy a data manipulation control 5, xioc - lower left x location 1, xioc - lower left x location 2, xioc - lower left x location 2, xioc - lower y position 2, xioc - lower left x location 3, xioc - lower left x location 4, xioc - lower y position 6, xioc - lower y position 7, xioc - lower y position 8, xtloc - lower y position 1, yien - length y TITLE (90 degrees to horizontal) 1, xioc - lower y position 2, xioc - lower y position 2, xioc - lower y position 2, xioc - lower w position 2, xioc - lower left x position 2, xioc - lower left x position 3, xioc - lower left x position 4, xioc - lower left x position 2, xioc - lower left x position 3, xioc - lower left x position 4, xioc - lower left x position 2, xioc - lower left x position 3, xioc - l	Apr 19	16:41 1988 tlran.con Page l		
munders parallel swits and the same of the space of the s	, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,	L PLOT CONTROL PARAMETERS t number of data files plotted on one plot wais lencth in inches - axis lencth in inches - axis suppression. (0) supress, (1) box, sampling frequency flag (- x axis exponential control (- x axis exponential control - x axis suppression in user units - x axis supple increment in user units		<u> </u>
filin- input d.a. file name SETUP FOR INDIVIDUAL PLOT X3 - lower left corner x position y3 - lower left corner y position y3 - lower left corner y position ya - lower left corner y position ymax ymax ymax ymax ymax ymin ymax ymin ym	20., 0, 5., 3, .125 1,			(11) (13) (14) (15) (15) (17)
SETUP FOR INDIVIDUAL PLOT x3 - lower left corner x position y3 - lower left corner y position y3 - lower left corner y position ymax ymin ytic nrot size dec justify nyp - number of places after decimal place hopy - vais exponential control nexpy- y axis exponential control ySTRNG - on axis desired MANOR TITLE (B) desired MANOR TITLE (C) desired MINOR TITLE (C) 1 Shallow Water (8,10,50,1500) T.C. desired MINOR TITLE (S) Hz, SD: 25 m, RD: 25 m, GAUSS (0,0) titsiz - title size xloc - lower left x location desired Y TITLE (90 degrees to horizontal) xtloc - lower left y location desired Y TITLE (90 degrees to horizontal) xtloc - lower right x position ytloc - lower position ytloc - lower y position yloc - lower y position	* **	a. file name		(19)
<pre>notot- total number of points plotted for partial plot. (nskip- plotting point increment ()</pre>	1.5, 5.0, 5.0, 5.0, 1.0, 1.0, 1.0, 1.1, 1.1, 1.5, 1.5, 1.5, 1.5, 1.5, 1.5	SETUP FOR INDIVIDUAL PLOT x3 - lower left corner x position y3 - lower left corner y position y1anax ymax ymax ymin ytic nrot size dec justify nyp - number of places after decimal place nlog - data manipulation control nexpy- y axis exponential desired MAJOR TITLE tel: Shallow Water (8,10,50,1500) T.C. desired MAJOR TITLE tel: Shallow Water (8,10,50,1500) T.C. desired MAJOR TITLE tel: Shallow Water (8,10,50,1500) T.C. desired MAJOR TITLE xloc - lower left y location yloc - lower left y location yloc - lower right x position yloc - lower right x position yloc - lower y position	(25) (3) (3) (3) (3) (3) (3) (3) (3) (3) (3	
	ò~`	partial	(36)	

Apr 19 16:41 1988 tlran.con Page 2 0, numsyn-symbol number for point plotting 0.15, symsiz-symbol size in inches 0.0, xoff-x offset in user units 0.0, yoff-y offset in user units 0,0, mdash - number of dashed lines for this plot		(37) (38) (39) (40) (41)	
	Apr 19 16:41 1988 tlran.con Page 2		



11.2. Wedge-Shaped Ocean with Penetrable Bottom

The second example tries to repeat the results by Jensen and Kuperman [17]. The environment consists of an initial 5 km stretch of 200 m depth followed by a bottom slope of 1.55° . The source used is the standard Gaussian source (the half width is not given in [17]), at 112 m depth, the frequency is 25 Hz. The maximum water depth is 200 m with a sediment layer extending to a depth of 800 m.

The program is such that the contour plot extends in range from the source to the maximum range, and in depth from the surface to the maximum depth. The maximum depth is the maximum sum of the water depth, sediment/bottom and subbottom heights.

The transmission loss versus depth extends in depth from the surface to the maximum depth like in the contour plot, and all mesh points are used. The transmission loss versus depth is interpolated in range when the selected range is not a range mesh point.

The contour plot is presented below. One finds good agreement with [17] although the contour routines are different. A copy of the input file as well as the script and plot control files and the sector information output file are following. This job takes 50 minutes to run on a Sun Workstation 3/50 (Sun Workstation is a registered trademark of Sun Microsystems, Inc).

```
number of receiver depths, of selected ranges for tl vs range or depth
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         number of points in the water sound velocity profile (integer)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        source O-gaussian, 1-field given in file, 2-greene, 3-thompson
                                                                                                                                                                                                                                                                                                                                                             transmission loss versus range at selected depths transmission loss versus depth at selected ranges
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              input filename containing the starting field (source=1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      half beam width, beam tilt from horizontal in degrees
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         operational mode of parabolic equation model (0 or 1)
                                                                                                     # input file for the program pe (MPL's pareq version)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          number of ranges, number of depths for contour plot
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    sound velocity profile : depth in m, velocity in m/
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   sediment heigth in m, sediment density in g/cm^{**3}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  input receiver depth array for tl vs range in m
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       input selected range array for tl vs depth in m
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     reference sound speed in m/s (can be 0, <0, >0)
                                                                                                                                                                                                                                                    enter the 6 file names to save the output data
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    flag for spreading (0-cylindrical 1-spherical)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         # tranform size (0 means that pe takes care of
                                                                                                                                                                                                                                                                                     ###### 5 characters is the required format
outfil0 # sectors information file
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             range step (0 means it is variable in pe)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        water depth in m, starting range in km
                                                                                                                                                                                                                                                                                                                                                                                                                                 sio data file for contour
sio data file for the field
   example. 2 Page 1
                                                                                                                                                                                                                                                                                                                               sectors information file
                                                                                                                                                                                   title of the input data file
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       maximum range of track in km
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              number of sectors (integer)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       output range distance in m
                                                                                                                                                                                                                    coastal slab
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       repeat for each sector :
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   source depth in m
Apr 20 09:14 1988
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           frequency in Hz
                                                                                                                                                                                                                       Saclant Test
                                                                                                                                                                                                                                                                                                                                                                                                                                 outfil4 #
```

```
25.2
                                                                         number of points in the sediment sound velocity profile (integer)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      number of points in the sediment sound velocity profile (integer)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            number of points in the sediment sound velocity profile (integer)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        number of points in the water sound velocity profile (integer)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  number of points in the water sound velocity profile (integer)
                                                                                                                                         sound speed profile in sediment : depth in m, velocity in m/s
1704.5
                                                                                                                                                                                                                                                                    subbottom density in g/cm**3 and attenuation in dB/wavelength
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             subbottom density in g/cm**3 and attenuation in dB/wavelength
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             subbottom density in g/cm**3 and attenuation in dB/wavelength
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     sound speed profile in sediment : depth in m, velocity in 1704.5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      sound speed profile in sediment : depth in m, velocity in 1704.5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           sound velocity profile : depth in m, velocity in m/s
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        sound velocity profile : depth in m, velocity in m/s
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   * sediment heigth in m, sediment density in g/cm**3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            sediment heigth in m, sediment density in g/cm**3
# attenuation in sediment in dB/wavelength
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      attenuation in sediment in dB/wavelength
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            attenuation in sediment in dB/wavelength
                                                                                                                                                                                                                                                                                                                                                                                                                       water depth in m, starting range in km
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    water depth in m, starting range in km
                                                                                                                                                                                                                                                                                                                                                 sound velocity in subbottom m/sec
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       sound velocity in subbottom m/sec
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       sound velocity in subbottom m/sec
```

example. 2 Page

Apr 20 09:14 1988

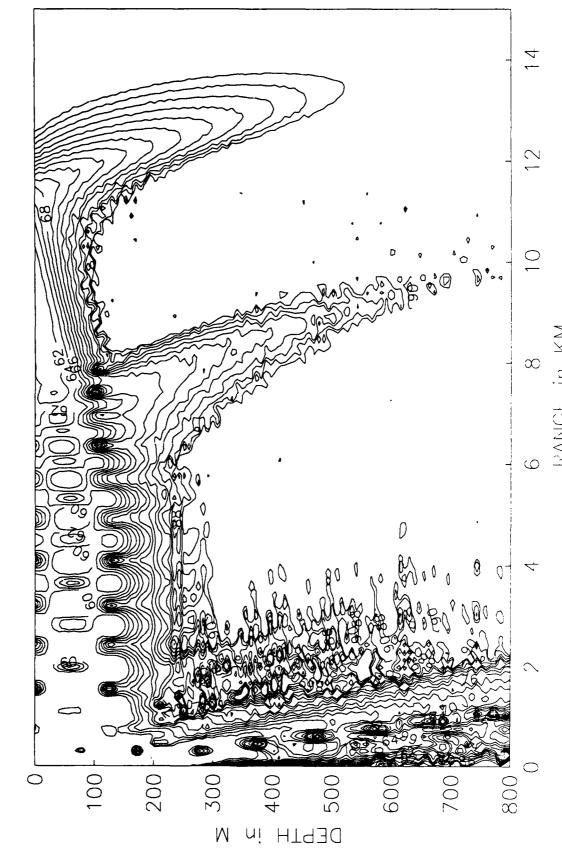
Feb 8 10:05 1988 outfill Page 2 0.0 M SOUND SPEED PROFILE IN SEDIMENT # 2 AT RANGE 5000.0 M SOUND SPEED PROFILE IN SEDIMENT # 3 AT RANGE 12500.0 M 0.0 M SOUND SPEED PROFILE IN WATER # 2 AT RANGE 5000.0 M SOUND SPEED PROFILE IN WATER # 3 AT RANGE 12500.0 M SOUND SPEED PROPILE IN SEDIMENT # 1 AT RANGE SOUND SPEED PROFILE IN WATER # 1 AT RANGE Feb 8 10:05 1988 outfill Page l SEDIMENT DENSITY = 1.150 SEDIMENT ATTERUATION = 0.500 NO SUBBOTTOM SEDIMENT DENSITY = 1.150 SEDIMENT ATTENUATION = 0.500 NO SUBBOTTOM SEDIMENT DENSITY = 1.150 SEDIMENT ATTENUATION = 0.500 SPEED(M/S) 1704.50 1704.50 SPEED(M/S) 1704.50 1704.50 SPEED(M/S) 1500.00 1500.00 DEPTH(M) 0.00 600.00 DEPTH(M) 0.00 200.00 DEPTH(M) 0.00 600.00 DEPTH(M) 0.00 1.00 DEPTH(M) 0.00 799.00 DEPTH(M) 0.00 200.00

NO SUBBOTTOM

```
# title - label centered above plot
EXAMPLE 2 : COASTAL SLAB [17]
# caption - label at bottom left corner of plot ( left justified )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                             - min x axis label value
- max x axis label value
- min y axis label value
- max y axis label value
- max y axis label value
contour - number of contour levels (if 0 program will choose)
codesw - togale for line weighting. must have 'connum' of codes.
Contour levels if specified by user
                                                                                                                                                                                                                                                                                                                                  colnum - # of columns for the input array (neg = flip vertical) rownum - # of rows for the input array (neg = flip horizontal) rotnum - number of 90 degree clockwise rotations
                                                                                                                                                                                                                                                       xlabsz - Size of x axis label
ylabsz - Size of y axis label
levsiz - Size of level labels
scalef - Scale of level labels (level value / scalef)
                                                                                                                                                                         ylab - y axis label - centered at left side of plot
                                                                                                                                            xlab - x axis label - centered at bottom of plot
                                               Contour draft plot control file
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Codesw weighting values
Apr 19 16:50 1988 pltconl Page l
                                                                                                                                                                                                                         titsiz - Size of Title
capsiz - Size of Caption
                                                                                                                                                                                                                                                                                                                                                                                                  length of the x-axis heigth of the y-axix x-org y-org Plot Parameters xmin - min x axis la
                                                                                                                                                                                                                                                                                                                                                                                    Plot Axis Parameter
                                                                                                                                                                                                                                                                                                                       Data Manipulation
                                                                                                                                                                                                            Label Sizes
                                                               Labels
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               xamax
nin
ymax
                                                                                                                                                            RANGE in KM
                                                                                                                                                                                          DEPTH in M
                                                                                                                                                                                                                                                                                                                                    100,
-100,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                8.0,
1.5,
```

pltconl Page

Apr 19 16:50 1988



EXAMPLE 2 : COASTAL SLAB [17]

11.3. Deep Water Example I (Range Independent)

This example is of deep water propagation over a range of $60 \, km$, the water depth is $2000 \, m$, the frequency is $100 \, Hz$ and the source is a 2° narrow and 8° tilted Gaussian source at $250 \, m$ depth [1]. One finds once again agreement between the MPL's PE program and [1]. Script, input, plot control files and plots follow. This run takes 30 minutes on a Sun Workstation 3/50 (Sun Workstation is a registered trademark of Sun Microsystems, Inc).

```
first demultiplex the channel 1 to yield the proper units in km for the plotting package and clip the transmission loss values between 70 and 130 dB
                                                                                                                                                                                                                      demux 1 outfilbsio templ
demux 2 outfilbsio temp2
demux 3 outfilbsio temp3
multc. 001 temp1 temp
clip 130 70 temp2 temp2
clip 130 70 temp3 temp3
mux temp temp22 temp1
mux temp temp23 temp3
  scr Page 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           contour (< INN > contourplot pltconl outfild
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                2n << INN > example3.plt2
tlran2.con
                                                                                                                                                                                                                                                                                                                                                                                                                                      2n << INN > example3.plt1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             plotwin example3.plt2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 plotwin example3.plt1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             plotwin contourplot
Apr 20 08:39 1988
                                                             EXAMPLE 3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  outfilbsiobis
outfilbsiobis
INN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              outfilbsiobis
outfilbsiobis
                                                                                                                                                                                                                                                                                                                                                                                                      plot
                                                                                                                                                                                                                                                                                                                                                                                                                                                      tlranl.con
n
                                                                                            pe << INN example.3 INN
                                                                                                                                                                                                                                                                                                                                                                          rm temp*
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               e N
```

```
number of receiver depths, of selected ranges for tl vs range or depth
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              number of points in the water sound velocity profile (integer)
                                                                                                                                                                                                                                                                                                                                            transmission loss versus range at selected depths transmission loss versus depth at selected ranges sio data file for contour sio field tile
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       source funtion (0-gaussian, 1-mxdal, 2-greene, 3-thompson)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 operational mode of parabolic equation model (0 or 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        half beam width, beam tilt from horizontal in degrees
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            sound velocity profile : depth in m, velocity in m/s
                                                                                                      input file for the program pe (MPL's pareq version)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  number of ranges, number of depths for contour plot
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  tranform size (0 means that pe takes care of it)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       input selected range array for tl vs depth in m
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           reference Jound speed in m/s (can be 0, (0, )0)
                                                                                                                                                                                                                                            # enter the 6 file names to save the output data
####### 7 characters is the required format
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     flag for spreading (0-cylindrical 1-spherical)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   input receiver depth array for tl vs range in
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         range step (O means it is variable in pe)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             water depth in m, starting range in km
                                                                                                                                                                                                                                                                                                                   # sectors information file
Apr 20 08:48 1988 example.3 Page 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            lower and upper modes (integers)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   maximum range of track in km
                                                                                                                                                                              of the input data file
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        number of sectors (integer)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            output range distance in m
                                                                                                                                                                                                                : Deep Water
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        repeat for each sector :
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              source depth in m
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          frequency in Hz
                                                                                                                                                                              title
                                                                                                                                                                                                                Saclant
                                                                                                                                                                                                                                                                                                                                                     out filb
                                                                                                                                                                                                                                                                                                                                                                                                                    outfild
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  8
```

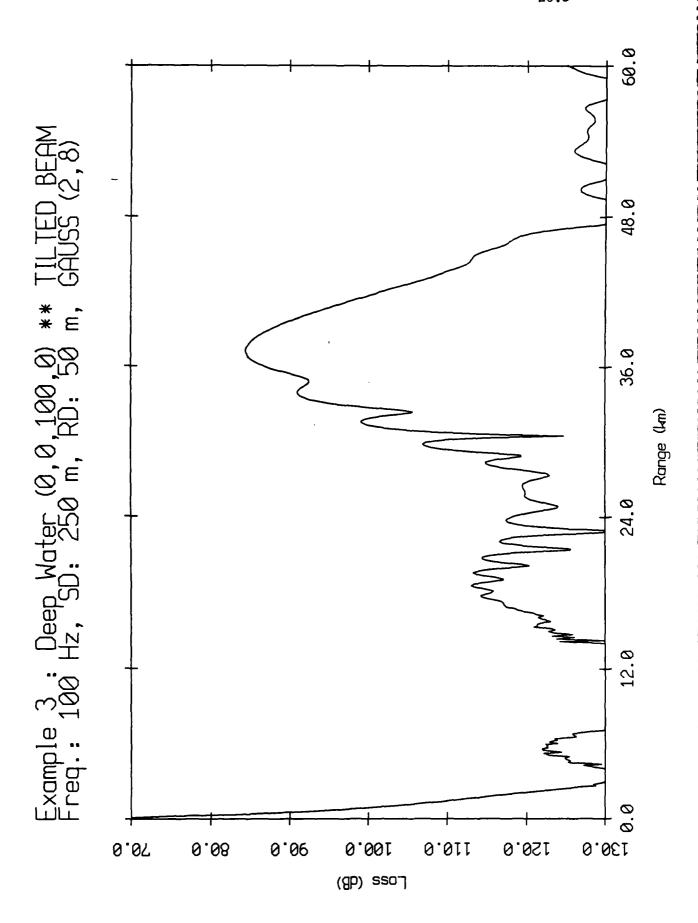
```
1000. 1470.
1000. 1476.
2000. 1476.
2000. 1476.
2000. 1476.
2000. 1476.
2000. 15.
# sediment heigth in m, sediment density in g/cm**3
# attenuation in sediment in dB/wavelength
0.5
# sound sed profile in sediment : depth in m, velocity in m/s
0.0. 1475.
2.0. 1670.
2.0 0.1
# sound velocity in g/cm**3 and attenuation in dB/wavelength
2.0 0.1
# sound velocity in subbottom m/sec
1800.
```

Apr 20 08:48 1988 example.3 Page 2

<u></u>		·		· · · · · · · · · · · · · · · · · · ·		 	 -
	×		D. 0				
	0.0 A						
	AT RANGE		AT RANGE				
	l AI		- -		•		
	WATER #	<u>શ</u> ે	IMENT	0.500	SUBBOTTOM DENSITY = 2.000 SUBBOTTOM ATTENUATION = 0.100 SUBBOTTOM SOUND SPEED = 1800.000		
	SOUND SPEED PROFILE IN WATER #	SPEED(M/S) 1480.00 1476.00 1470.00 1476.00 1490.00	OFILE IN SEI SPEED(M/S) 1475.00 1600.00	SEDIMENT DENSITY - 1.500 SEDIMENT ATTENUATION - 0.500	ITY = 2.(NUATION = D SPEED =		
	SPEED PRO		SPEED PRH (M) .00	NT DENSI'	TOM DENS TOM ATTEI TOM SOUN		
	SOUND	DEPTH(M) 0.00 100.00 500.00 1000.00	SOUND SPEET DEPTH(M) 0.00 100.00	SEDIME	SUBBOT SUBBOT SUBBOT		

GLOBAL PLOT CONTROL PARAMETERS numplt - number of data files plotted on one plot xlen x axis length in inches noaxe - axis suppression. (0) supress, (1) box, nsf - sampling frequency flag nexx - x axis exponential control lWEPENDENT X AXIS PARAMETERS xorg - x axis origin in user units xinc - x axis sample increment in user units xxinc - x axis sample increment in user units xxinc - x tic mark spacing in user units xxinc - x tic mark spacing in user units xxinc - x tic mark spacing in user units xxinc - x tic mark spacing in user units xxinc - x tic mark spacing in user units ylen to places after the decimal point FILE PARAMETERS filin - input d.a. file name SETUP FOR INDIVIDUAL PLOT x3 - lower left corner x position ylen - length of axis yman yen - lower left corner x position ylen - length of axis ymax ymin ylic nrot size dec justify npc - lower left control nexpy - y axis exponential desired MANOR TITLE led 3: Deep Water (0,0,100,0) ** TILTED BEAM desired MANOR TITLE led 3: Deep Water (0,0,100,0) ** TILTED BEAM desired HANOR TITLE size xloc - lower left x location yloc - lower left x location desired x TITLE (90 degrees to horizontal) xxloc - lower right x position				
NATIS AXIS AXIS AXIS AXIS AXIS AXIS AXIS SIZE JUST TILL FILL FILL YIEN ASIZE GEC ASIZE GEC ASIZE ASIZE GEC ASIZE GEC ASIZE GEC ASIZE GEC ASIZE ASIZE GEC ASIZE A	-	AAL PLOT CONTROL PARAMETERS plt- number of data files plotted on one plot n- x axis length in inches ke - axis suppression. (0) supress, (1) box, (2) lower, - sampling frequency flag px- x axis exponential control	(3) mid	<u> 66€66</u>
AANS AANS AMINA AANS AANS SIZE JUST JUST FILE FILE FILE FILE FILE FILE FILE FILE		ENDENT X x axis x axis		<u>6</u> 6
just property of the property	- X X E 01	S SCALING PARAMEIERS x-x maximum in user units n-x minimum in user units ic-x tic mark spacing in user units bers parallel	22	(11) (12) (13) (14) (15)
SETUP FOR INDIVIDUAL PLOT x3 - lower left corner x position y3 - lower left corner y position ylen - length of axis ymax ymax ymin ytic nrot size dec justify nyp - number of places after decimal nlog - data manipulation control nexpy- y axis exponential log - data manipulation nexpy- y axis exponential nlog - data manipulation desired MAJOR TITLE left y location yloc - lower right x position	just nxp- FILE fili	tify number of places after the decimal point E PARAMETERS in- input d.a. file name		(16) (17) (19)
ytsize- ytsize- AXIS LAB XSTRNG- (km) chanl - chanl - nreal- ndpo-fi	A V V V V V V V V V V V V V V V V V V V	P FOR INDIVIDUAL PLOT lower left corner x position lower left corner y position ytic nrot ytic nrot ytic nrot ytic nrot y axis exponential control y y axis exponential control NG - on axis red MAJOR TITLE Deep Water (0,0,100,0) ** TILTED BEAM RA. 5D: 250 m, RD: 50 m, GAUSS (2,8) iz - title size lower left x location c - lower left y location c - lower left y location c - lower right x position cc - lower y position cc - lower plot to plot cd - channel number to plot d - channel to do math with al - flag for plotting real or imaginary part-also da lists point plotted for partial fills plotting lists point number of points plotted for partial fills plotting lists point number of points plotted for partial fills plotting lists point number of points plotted for partial fills plotting lists point number of points plotted for partial fills plotting lists point plotted for partial fills plotting lists point number to plot for plotting real or imaginary part-also da lists point plotted for partial fills plotting	(25) (35) (35) (35) (35) (35) (35) (35) (3	

Apr 19 17:29 1988 tlranl.con Page 2 0, numsyn- symbol number for point plotting 0.15, symsiz- symbol size in inches 0.0, xoff- x offset in user units 0.0, yoff- y offset in user units 0, ndash - number of dashed lines for this plot



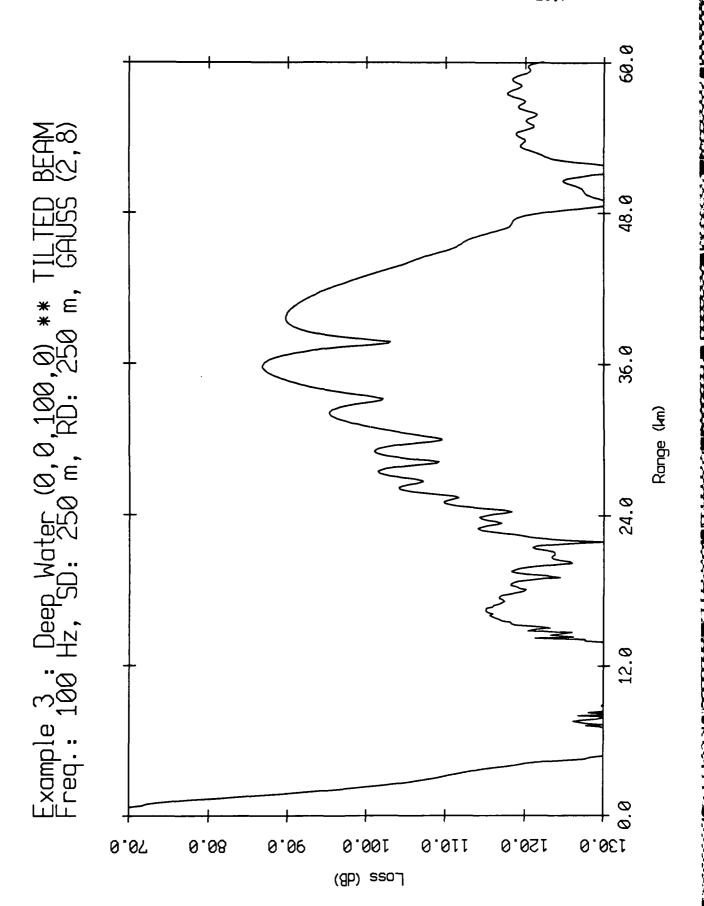
-1, 8.0, 1, 0,	GLOBAL PLOT CONTROL PARAMETERS numplt—number of data files plotted on one plot xlen—x axis length in inches noaxe—axis suppression. (0) supress, (1) box, (2) lower, nsf—sampling frequency flag nexpx—x axis exponential control	, (3) mid	<u>66€66</u>
, 0, 1,	_ 0 00 0		86
60., 0, 112., 3, 125	AAIS SCALLING FARAMENTERS XMAX- X maximum in user units xmin- X minimum in user units xtic- X tic mark spacing in user units numbers parallel size instify		(12) (12) (13) (14) (15)
ì	DESTRICT OF PLACES after the decimal point FILE PARAMETERS filin—input d.a. file name		(17)
1.5, 1.0, 5.0, 70.0, 130.0,	SETUP FOR INDIVIDUAL PLOT X3 - Lower left corner x position y3 - Lower left corner y position ylen - length of axis ymax ymin yric yric	<u> </u>	
	2 D C C X F	1 3333333	
Loss (di # c Example # Freq.:] 0.20, t 1.5, x]	desired MAJOR TITLE desired MAJOR TITLE desired MINOR TITLE desired MINOR TITLE : 100 Hz, SD: 250 m, RD: 250 m, GAUSS (2,8) titsiz - title size xloc - lower left x location yloc - lower left y location desired Y TITLE (90 degrees to horizontal)	(16) (18) (20) (21) (23) (23)	
	xtloc - lower right x position ytloc - lower y position ytsize- y title size AXIS LABEL PARAMFTERS AXIS LABEL PARAMFTERS	(25) (26) (27) (29)	
3, 1, -1, 0,	<pre>(ww) clan! - channel number to plot chan2 - channel to do math with nreal- flag for plotting real or imaginary part-also da nap0- first point plotted for partial file plotting ndtot- total number of points plotted for partial plot. nskip- plotting point increment</pre>	(31) (32) (33) (34) (35)	

(41) (41) (41)

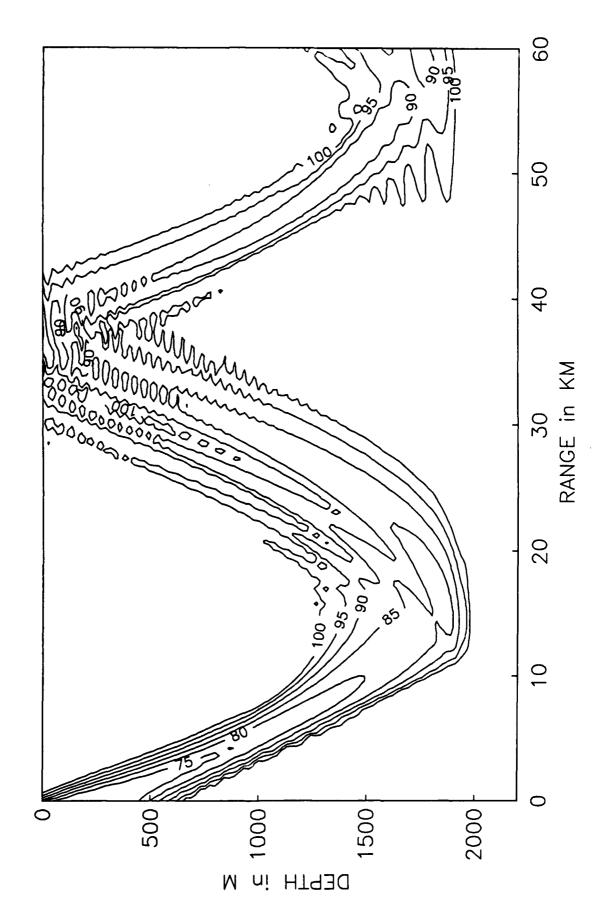
numsyn- symbol number for point plotting symsiz- symbol size in inches xoff- x offset in user units yoff- y offset in user units ndash - number of dashed lines for this plot

0, 0.15, 0.0, 0.0,

Apr 19 17:30 1988 tlran2.con Page 2



```
caption - label at bottom left corner of plot ( left justified )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               connum - number of contour levels (if 0 program will choose) codesw - toggle for line weighting. must have 'connum' of codes. Contour levels if specified by user
                                                                                                                                                                                                                                                                                                                                                                                                                             colnum - # of columns for the input array (neg = flip vertical)
rownum - # of rows for the input array (neg = flip horizontal)
rotnum - number of 90 degree clockwise rotations
                                                                                                                                                                                                                                                                                    titsiz - Size of Title
capsiz - Size of Caption
xlabsz - Size of x axis label
ylabsz - Size of y axis label
levsiz - Size of level labels
scalef - Scale of level labels
                                                                                                                                                                                                                       ylab - y axis label - centered at left side of plot
                                                                                                                                                                                 xlab - x axis label - centered at bottom of plot
                                                                                                    title - label centered above plot
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ymin - min y axis label value
max y axis label value
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                - min x axis label value
- max x axis label value
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Codesw weighting values
                                                    Contour draft plot control file Labels
Apr 19 17:37 1988 pltconl Page 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             length of the x-axis
heigth of the y-axix
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              Plot Axis Parameter
                                                                                                                                                                                                                                                                                                                                                                                                                Data Manipulation
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               y-org
Plot Parameters
                                                                                                                                                                                                                                                                     Label Sizes
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              K-org
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          хшах
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  утах
                                                                                                                                                                                                         RANGE in KM
                                                                                                                                                                                                                                                 DEPTH in M
                                                                                                                                                                                                                                                                                                                                                                                                                                100,
-100,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        60,
2200.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               8.0,
1.5,
```



EXAMPLE 3 : DEEP WATER (0,0,100,0) ** TILTED BEAM (2,8)

11.4. Deep Water Example II (Range Independent)

This last example is of deep water propagation at 100 Hz in a range independent medium [1]. The source, 250 meter deep is a Gaussian source with a 2° width and a 8° tilt. The maximum water depth is 2000 m with a 100 m sediment layer and a subbottom. The script produces a plot of transmission loss versus range, a plot of transmission loss versus depth and a partial contour plot. One can see agreement with [1]. Script, input, plot control files and plots follow. This run takes 30 minutes on a Sun Worstation 3/50 (Sun Workstation is a registered trademark of Sun Microsystems, Inc).

Apr 20 08:50 1988 script Page 1
EXAMPLE 4
example.4 INN
part the data and plot the results of transmission loss versus range
part 281 133 outfil2sio temp demux 1 temp templ multc. 001 templ temp3 demux 2 temp temp2 mux temp3 temp2 zn << INN > tlran.plt3 tlranl.con
temp temp
plotwin tlran.plt3
part the data and plot the results of transmission loss versus depth
part 1 90 outfil3sio tdemp 2n << INN > tlrde.plt3 trdep.con
tdemp tdemp tdemp inn
plotwin tirde.plt3
script to treat the contour plot
part 67 33 outfil4 tempcont getchan tempcont tempcol 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 contour < INN > contourplot pltconl tempco
inn plotwin contourplot

```
Feb 8 09:12 1988 getchan Page 1.

# get_chans - make a new sio data file from selected channels of an old is single as sind data file

If (# largy < 3) then echo! ', echo 'use: get_chans infile outfile chan chand ...', echo! ', echo! '; echo "; not found.", echo! ', exit

if (1 - 0 1) then echo!

echo! ', echo "; not found.", echo '', exit

echo! ', echo "; not file-$2

set infile-$1 outfile-$2

set infile-$1 outfile-$2

set infile soutfile

echo getting channel $1 from $infile

demux $1 sinfile $5

mux $cutfile $cutfile $cutfile $cutfile $cutfile $cutfile $cutfile $cutfile $cu
```

```
number of receiver depths, of selected ranges for tl vs range or depth
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              number of points in the water sound velocity profile (integer)
                                                                                                                                                                                                                                                                                                   transmission loss versus range at selected depths transmission loss versus depth at selected ranges
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   source funtion (0-gaussian,1-modal,2-greene,3-thompson)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            operational mode of parabolic equation model (0 or 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          half beam width, beam tilt from horizontal in degrees
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       # sound velocity profile : depth in m, velocity in m/s 0. 1480. 1476. 500 1470
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      number of ranges, number of depths for contour plot
                                                                                            input file for the program pe (MPL's pareg version)
                                                                                                                                                                                                                                                                                                                                                                                                  # tranform size (0 means that pe takes care of it)
0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             input selected range array for tl vs depth in m
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             reference sound speed in m/s (can be 0, <0, >0)
                                                                                                                                                                                                               we 6 file names to save the output data
characters is the required format
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     flag for spreading (0-cylindrical 1-spherical)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               input receiver depth array for tl vs range in
                                                                                                                                                                                                                                                                                                                                                                                                                                                                               # range step (0 means it is variable in pe)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   name of the sio data file for the field
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    water depth in m, starting range in km
                                                                                                                                                                                                                                                                                                                                                          sio data file for contour
sio field file
Apr 20 09:16 1988 example.4 Page 1
                                                                                                                                                                                                                                                                             sectors information file
                                                                                                                                                     the input data file
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     maximum range of track in km
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    number of sectors (integer)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    output range distance in m
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              repeat for each sector :
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    source depth in m
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             frequency in Hz
                                                                                                                                                                                                                                                                                                   outfil2 1
                                                                                                                                                                                                                                                                                                                                 outfil3
                                                                                                                                                                                                                                                                                                                                                                  outfil4
                                                                                                                                                                                                                                                                        out fill
                                                                                                                                                                                      Saclant
```

```
Apr 20 09:16 1988 example.4 Page 2

1000. 1476.
2000. 1490.
# sediment heigth in m, sediment density in g/cm**3
100. 1.5
# attenuation in sediment in dB/wavelength
0.5
# number of points in the sediment sound velocity profile (integer)
2 sound speed profile in sediment : depth in m, velocity in m/s
# sound speed profile in sediment in dB/wavelength
0. 1475.
100. 1600.
# subbottom density in g/cm**3 and attenuation in dB/wavelength
2.0 0.1
# sound velocity in subbottom m/sec
```

					_	
	_	E 0.				
	0					
	AT RANGE	l at range				
1988 outfill Page l	SOUND SPEED PROFILE IN WATER # 1 A DEPTH(M) SPEED(M/S) 0.00 1476.00 1000.00 1476.00 1470.00 2000.00 1490.00	SOUND SPEED PROFILE IN SEDIMENT # 1 DEPTH(M) SPEED(M/S) 0.00 1475.00 100.00 1600.00	SEDIMENT DENSITY = 1.500 SEDIMENT ATTENUATION = 0.500 SUBBOTTOM DENSITY = 2.000	UND SPEED = 1800.000		
Feb 8 09:02 1988	SOUND SPEED P DEPTH(M) 0.00 100.00 500.00 2000.00	SOUND SPEED P DEPTH(M) 0.00 100.00	SEDIMENT DENSITY = 1.500 SEDIMENT ATTENUATION = 0. SUBBOTTOM DENSITY = 2.000	SUBBOTTOM SOL		

27	.5	
	• -	

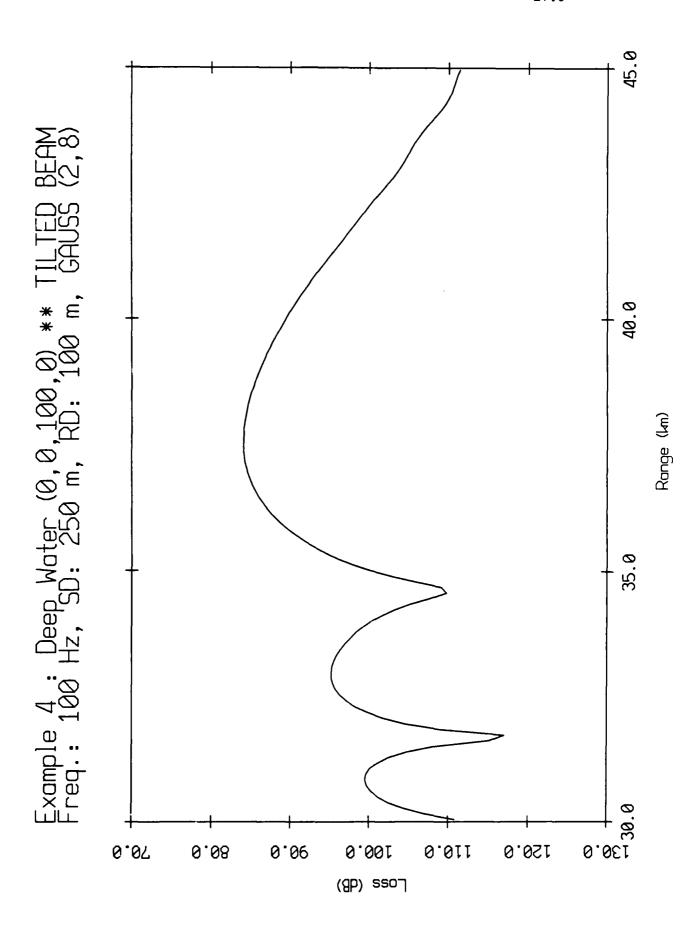
ANTERNAL ESPECIAL ESPECIAL ESPECIAL PROSESSA POSSESSA POSSESSA ESPECIAL ESPECIAL PROSESSA PROSESSA PROSESSA P

Apr 20	Apr 20 08:51 1988 tlranl.con Page l		Apr 20 08:51 1988 tlranl.con Page 2
11, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,	GLOBAL PLOT CONTROL PARAMETERS numplt- number of data files plotted on one plot xlen - x axis length in inches noaxe - axis suppression (0) supress, (1) box, (2) lower, (3) mid nsf- sampling frequency flag nexpx- x axis exponential control INDEPREENT XAIS PARAMETERS xorg - x axis sample increment in user units XINC- x axis sample increment in user units AXIS SCALING PARAMETERS xmax- x maximum in user units xmin- x minimum in user units xxic- x tic mark spacing in user units xxic- x tic mark spacing in user units	පිටිදිලිම මම මුදිලිදි දිවිදිලිම	0, numsyn-symbol number for point 0.15, symsiz-symbol size in inches 0.0, xoff-x offset in user units 0.0, yoff-y offset in user units 0.0, mdash - number of dashed lines
.125 2, 1,	size justify nxp- number of places after the decimal point FILE PARAMETERS filin- input d.a. file name	(15) (17) (19)	
SE 11.5, x3 11.0, y3 11.0, y3 13.0, y3 15.0, y3 15.0, y3 15.0, y3 15.0, y3 15.0, y4 15.0, y5	SETUP FOR INDIVIDUAL PLOT x3 - lower left corner x position y3 - lower left corner y position year ymax ymax ymin ytic nrot size app - number of places after decimal place nlog - data manipulation control nexpy- y axis exponential control nexpy- y axis exponential control yerrang - on axis desired MAJOR TITLE e 4 : Deep Water (0,0,100,0) ** TILTED BEAM desired MINOR TITLE titsiz - title size xloc - lower left x location yloc - lower left x location yloc - lower left x location yloc - lower right x position ytloc - lower y position ytlos - lower y position		
	nreal ndp0- ndtot nskip-		

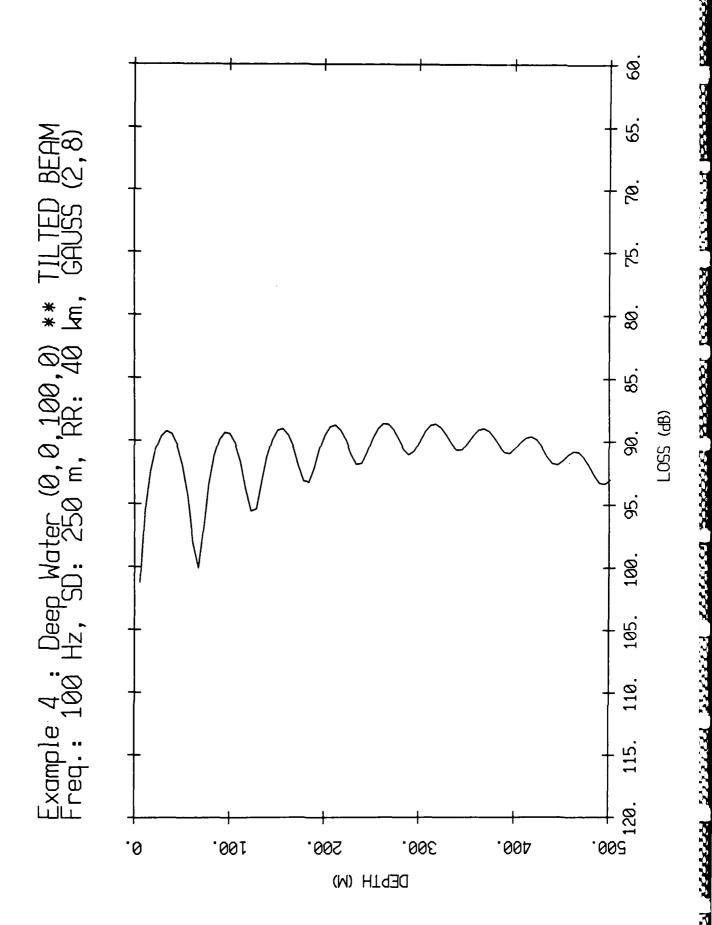
<u> 1888 YANGAR KANDAN BANDAN BANDAN ANDAN BANDAN BAN</u>

£6333 £6333

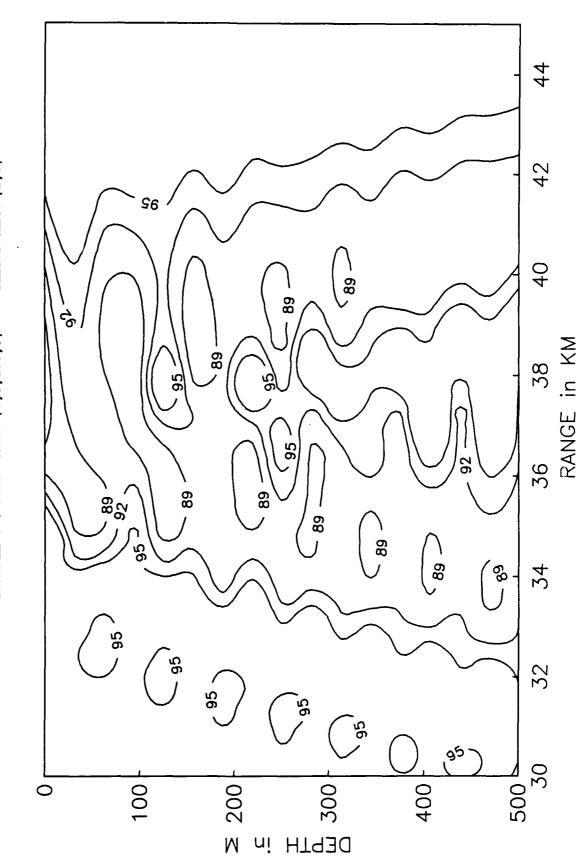
numsyn- symbol number for point plotting symsiz- symbol size in inches xoff- x offset in user units yoff- y offset in user units ndash - number of dashed lines for this plot



	(33) (38) (40) (41)	
Apr 20 08:53 1988 trdep.con Page 2	0, numsyn- symbol number for point plotting 0.15, symsiz- symbol size in inches 0.0, xoff- x offset in user units 0.0, yoff- y offset in user units 0, ndash - number of dashed lines for this plot	



```
caption - label at bottom left corner of plot ( left justified )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  - min x axis label value
- max x axis label value
- min y axis label value
- max y axis label value
- max y axis label value
connum - number of contour levels (if 0 program will choose)
codesw - toggle for line weighting. must have 'connum' of codes.
Contour levels if specified by user
                                                                                                                                                                                                                                                                                                                                                            colnum - # of columns for the input array (neg = flip vertical) rownum - # of rows for the input array (neg = flip horizontal) rotnum - number of 90 degree clockwise rotations
                                                                                                                                                                                                                                      titsiz - Size of Title
capsiz - Size of Caption
Xlabsz - Size of x axis label
Ylabsz - Size of y axis label
levsiz - Size of level labels
scalef - Scale of level labels
Data Manipulation
                                                                                                                                                                                       ylab - y axis label - centered at left side of plot
                                                                                                                                                      xlab - x axis label - centered at bottom of plot
                                                                                       title - label centered above plot
                                                   Contour draft plot control file Labels
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 Codesw weighting values
Apr 20 08:53 1988 pltconl Page 1
                                                                                                                                                                                                                                                                                                                                                                                                                                     length of the x-axis
heigth of the y-axix
                                                                                                                                                                                                                                                                                                                                                                                                                 Plot Axis Parameter
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     x-org
Y-org
Plot Parameters
                                                                                                                                                                                                                             Label Sizes
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        Xmin
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        xmax
ymin
ymax
                                                                                                                                                                          ANGE in KM
                                                                                                                                                                                                           SEPTH in M
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  30,
500.,
**,
                                                                                                                                                                                                                                           1, 10, 115,
                                                                                                                                                                                                                                                                                                                                                               33,
-17,
                                                                                                                                                                                                                                                                                                                                                                                                                                 9.000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        83
83
84
95
95
```



EXAMPLE 4 : DEEP WATER (0,0,100,0) ** TILTED BEAM (2,8)

12. References

- [1] F.B. Jensen, M.G. Martinelli, "The SACLANTCEN Parabolic Equation Model (PAREQ)", (VAX/FPS Version), December 1985.
- [2] F. Jensen H. Kroll, "The Use of the Parabolic Equation Method in Sound Propagation Modelling" SACLANTCEN Memorandum SM-72, 15 August 1975.
- [3] W.A. Kuperman, "Models of Sound Propagation in the Ocean", Naval Research Review 3 vol XXXVII, pp 32-41, 1985.
- [4] F. Jensen, "Acoustic Propagation Modelling, Why Several Models?", SACLANTCEN CP-19, 1976.
- [5] F.D. Tappert, "Selected Applications of the Parabolic-Equation Method in Underwater Acoustics", International Workshop on Low Frequency Propagation and Noise, Vol I, Oct 14-19 1974, WoodsHole, Mass., Publ. 1977, pp 155-200.
- [6] F.D. Tappert, "The Parabolic Approximation Method", in Keller J.B. and Papadakis J.S. Eds, Wave Propagation and Underwater Acoustics, Lecture Notes in Physics 70. New York, Springer Verlag, 1977, pp 224-281.
- [7] D.J. Thomson, N.R. Chapman, "A Wide Angle Split Step Algorithm for the Parabolic Equation", JASA 74 (6), pp 1848-1854, December 1983.
- [8] M.D. Feit, J.A. Fleck Jr., "Light Propagation in the Graded-Index Optical Fiber", Applied Optics Vol 17 No 24, pp 3990-3998, 15 December 1978.
- [9] F.B. Jensen, H. Schmidt, "Review of Numerical Models in Underwater Acoustics Including Recently Developed Fast Field Program", SACLANTCEN Report SR-83, 15 December 1984.

- [10] H.K. Brock, "The AESD Parabolic Equation Model", NORDA Technical Note 12, January 1978.
- [11] S.T. MacDaniel, "Propagation of normal mode in the Parabolic Approximation", JASA 57 (2), pp 307-311, February 1975.
- [12] R.M. Fitzgerald, "Helmholtz Equation as an Initial Value Problem with Application to Acoustic Propagation", JASA 57 (4), pp 839-842, April 1975.
- [13] A.D. Pierce, "The Natural Reference Wavenumber for Parabolic Approximations in Ocean Acoustics", Comps & Maths with Appls, Vol 11 No 7/8, pp 831-841, 1985.
- [14] H.K. Brock, R.N. Buchal, C.W. Spofford, "Modifying the Sound Speed Profile to Improve the Accuracy of the Parabolic Equation Technique", JASA 62 (3), pp 543-552, September 1977.
- [15] L.E. Kinsler, A.R. Frey, Fundamentals of Acoustics, Wiley Eds
- [16] R.R. Greene, "The Rational Approximation to the Acoustic Wave Equation with Bottom Interaction", JASA 76 (6), pp 1764-1773, December 1984.
- [17] F.B. Jensen, W.A. Kuperman, "Sound Propagation in a Wedge-Shaped Ocean with a Penetrable Bottom", JASA 67 (5), pp 1564-1566, May 1980.